# MODELING RUNWAY CAPACITY USING MIXED INTEGER PROGRAMMING BASED ON FCFS AND AROT POLICIES

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# MODELING RUNWAY CAPACITY USING MIXED INTEGER PROGRAMMING BASED ON FCFS AND AROT POLICIES

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#### ABSTRACT

Air transportation are often used between islands and countries which have economic advantages over other types of transportation. Technology in aircraft enables an increase in demand from year to year. demand density creates a queue of aircraft on the runway. Airport faced challenge within a key bottleneck in the air transport system and runway schedulling. This study focuses on modeling runways using mixed integer programming with empirical studies at Juanda International Airport, Surabaya. We use runway capacity management baesd on schedulling approach, runway configuration and aricraft separation standard. This study is to minimize aircraft waiting time on the runway before departure and landing in the air with considerable reduction in delays and minimize in fuel cost. We proposed heuristic sequential approach based on FCFS and AROT policies. By conducting research using these methods, it is expected to obtain optimal results to facilitate decision making in daily operations.

**Keywords**: Air Transportation, Runway Capacity, Mixed Integer Programming, Aircraft Waiting Time.

# 1. INTRODUCTION

Transportation is one of the basic things in life today. Humans in the world are very dependent on how they move both people and goods from one place to another (Business Dictionary, 2011). Transportation is very important for a country. This is because economic growth is influenced by the ability of a country's transportation. Apart from supporting economic growth, transportation can also support aspects of Indonesian tourism.

In Indonesia, public transportation is one of the main focuses in government. Several types of public transportation were improved including air transportation. Air transport facilitates integration into the global economy and provides vital connectivity on a national, regional, and international scale (World Bank, 2017). The World Bank has funded air transportation projects for more than sixty years (World Bank, 2017) with efforts to help generate trade, promote tourism, and create job opportunities (World Bank, 2017). In addition, there are several reasons people

decide to choose a transport plane, namely air transportation is the most time-saving transportation compared to other types of transportation. The advanced technology in the aircraft allows this transport ten times faster than other types of transportation. However, the disadvantage of this transportation is that it is highly dependent on weather conditions. According to Graham (2014) an airport is a place that provides all the necessary infrastructure to allow passengers and shipments to transfer from other modes of transportation to air transportation and allow airlines to take off and land. The airport is divided into 2 based on the use of the facilities: the air side and the land side. Each airport consists of a runway (runway), taxiways, aircraft parking space (apron), gates, passenger and freight terminals, and ground transportation exchanges. The movement of airport aircraft in each region differs from one place to another. The movement of aircraft movements is based on several factors, such as the movement of the runway aircraft, safety factors, and others. Aircraft movement is a measure of the maximum number of aircraft operations that can be accommodated at an airport or airport component in one hour (Federal Aviation Administration, 1995).

Several airports in Indonesia that have contributed greatly to the increase in the number of passengers in Indonesia include Soekarno Hatta Airport, Juanda Airport, Hasanudin Airport, Ngurah Rai Airport, and Kualanamu Airport. Soekarno Hatta Airport as the busiest airport in Indonesia can depart and land as many as 50 million passengers a year. Juanda as the second busiest airport in Indonesia also has an important role. Although the number of passengers at Juanda is almost half that of Soekarno Hatta airport in Jakarta, the flow at the airport is still quite high compared to other airports. Juanda Airport is one of the airports in Indonesia which has a high target. According to the head manager, Juanda Airport has 28 capacities for normal flights and 5 capacities for emergencies. Juanda Airport can handle an average of 400 flights per day which includes flight arrivals and flight departures. However, sometimes there are delays that cause the flight flow not to function as scheduled.

One of the problems that occur at the airport is the runway sequencing problem (RSP).

Several studies discussing the RSP (runway sequencing problem) on a single runway are Julien et al (2017), Cetek (2014), Chao et al (2008), Irene et al (2007). According to Julien (2017) RSP consists of a sequence of runway operations that decide in which order and when each aircraft takes off, lands or crosses the runway by ensuring the level of safety in each sequence. In addition, Atkin et al (2007), Guepet (2016), Bennell et al (2011) and Lieder et al (2015) have also discussed ground routing problem (GRP) and runway sequencing problem (RSP). Deau et al (2008, 2009) discussed research on the sequential runway with the A-CDM approach. This study resolves the problem of the take-off sequence by targeting the take-off times (TTOTs) in the route model. Whereas Keith and Richard (2008) use mix integer programming (MIP) to integrate runway and ground routing in one model. According to Julien (2017) RSP consists of a sequence of runway operations that decide in which order and when each aircraft takes off, lands or crosses the runway by ensuring the level of safety in each sequence.

Therefore, this study will develop a model in calculating aircraft movements at airports using mixed integer programming with empirical studies at Juanda International Airport, Surabaya.

The paper is structured as follows in section 2 we state mathematical model formulation

Use indented instead of entered style for a new paragraph. When citing references, using the names of the authors and the year of publication is preferable. Here is an example. Smith (2005) suggested that the referencing style is one of the writing aspects that most students ignore

when preparing a paper. Correspondingly, the references should be listed based on alphabetical order of the first author's last name.

# 2. MATEMATICAL MODEL FORMULATION

# 2.1 Formulation of Runway Capacity

The calculation of delay for a runway that is used exclusively by arrival is calculated from this equation (adopted from Bazargan, 2010)

$$W_a = \frac{\lambda_a (\sigma_a^2 + 1/\mu_a^2)}{2(1 - \lambda_a/\mu_a)}$$

Where,

Wa = Mean delay for aircraft arrival

 $\lambda a = Mean arrival rate of the aircraft$ 

 $\mu a = Mean \text{ service}$  level of aircraft arrival or inverse mean service time

 $\sigma a =$  Standard deviation of the mean service arrival time of the aircraft.

The calculation of delay for the runway used for departure (Departure) is calculated from the equation:

$$W_d = \frac{\lambda_d (\sigma_d^2 + 1/\mu_d^2)}{2(1 - \lambda_d/\mu_d)}$$

Where,

Wd = Mean delay for airplane departure

 $\lambda d = Mean$  level of departure from the aircraft

 $\mu$ d = Mean service level for departure, or inverse average service time for departure

 $\sigma a =$ Standard deviation of the mean service time from flight departures

For Mixed Operations, arriving aircraft are usually given priority and this aircraft delay is given by the arrival equation, but the average delay for departure in this situation can be found from the equation:

$$W_d = \frac{\lambda_d(\sigma_j^2 + j^2)}{2(1 - \lambda_d^j)} + \frac{g(\sigma_f^2 + f^2)}{2(1 - \lambda_d^f)}$$

Where,

Wd = Mean delay for airplane departure

 $\lambda a = Mean arrival rate of the aircraft$ 

 $\lambda d = Mean$  level of departure from the aircraft

j = Mean interval of time between two successful departures

 $\sigma$ j = Standard deviation of the mean time intervals between successful departures

g = Average rate of gaps between successful arrivals

f = Mean value of the time interval with no take-off departures

 $\sigma f$  = Standard deviation from the time interval at which no departure has to be taken off

# 2.1 Heuristics Model

The heuristic approach in this study refers to Ghoniem (2014) who uses mixed integer programming (MIP), this model simultaneously searches for aircraft that enter the optimal aircraft runway by considering the separation policy between aircraft and the combination of arrival and departure. Ghoniem (2014) uses two runways in parallel and independently in carrying out the

model while in this study the focus is on a single runway. Therefore, this research model refers to Ghoniem's (2014) runway capacity management (RCM) research which is formulated as follows:

$$\begin{split} & \mininimize \sum_{j \in J} W_j(t_j - r_j) \\ & \text{With the attribute as follow:} \\ & \sum_{i \in N} Z_{ij} = 1, \quad \forall j \in J \\ & r_j \leq t_j \leq d_j, \quad \forall j \in J \\ & t_{j2} \geq t_{j1} + P_{j1j2} - M(1 - y_{j1j2}), \forall j_1 \in J, j_2 \in J, j_1 \neq j_2 \\ & y_{j1j2} + y_{j2j1} \geq Z_{ij1} + Z_{ij2} - 1, \forall i \in N, j_1 \in J, j_2 \in J, j_1 \neq j_2 \\ & y, z \text{ binary} \end{split}$$

Where,

- $C_i$  is the fuel consumption required by the aircraft according to the type and type of operation
- j∈J is each aircraft up to the number of J which carries several characteristics (i) the type of operation (i.e. departure or arrival) (ii) the type of aircraft weight (small, large, heavy) (iii) the ready time and duedate schedule of the aircraft is known (iv) the aircraft's fuel needs
- $r_j$  is the ready time / flight schedule at juanda airport
- $t_i$  is the time when the plane to j will be assigned to the runway
- $d_i$  is the duedate aircraft accessing the runway
- $P_{j1j2}$  is the minimum required separation time between consecutive assigned aircraft. This separation time uses the minimum flight rules set by ICAO
- M is a scalar number (large number) to help the program if airplane pairing is not selected. In finding M using  $M = d_{j1} r_{j2} + P_{j1j2}$
- $Z_{ij}$  has a binary value which means the number of runways used
- $y_{j1j2}$ has a binary value which shows the order of selecting the aircraft assigned to the runway, this shows the relationship between employee j1 and plane j2 if selected then it is 1 if not selected then it is zero (0)

#### 3. RESULT

This model minimizes the total cost of fuel that is obtained from the difference between the ready time and the time assigned to the runway. The fuel costs are assumed to be in the index as in table 1 below. The table shows that the fuel consumption required between departure (D) aircraft types is different from arrival (A) aircraft, which means that arrival requires a higher fuel consumption than departure so that the arrival of MIP can be selected first if there is an incident of two planes at the same time. at the same time there is departure and arrival. Likewise for small, large and heavy aircraft types, the model will choose the minimum result by not exceeding the duedate of each aircraft type. In determining the cost of fuel by type and type, researchers used a visual basic application (VBA) in Microsoft Excel.

Table 1. cost index and type of aircraft

index cost		tipe	of aircraft
S	1	D	1
L	1,5	А	1,5
н	1,75		

This model also considers the separation time or standard time between aircraft as defined by ICAO. If there is a Departure-Arrival aircraft, the minimum required separation time is 35 seconds. Meanwhile, for Arrival-Departure aircraft, it takes a minimum of 120 seconds between aircraft to be assigned to the runway. For the Departure-Departure type of operation, pay attention to the type of aircraft which can be seen in table 2 below. If the Arrival-Arrival type of operation can be seen in table 5.3. When assigning the aircraft, it is necessary to pay attention to the type of heavy or small or large aircraft that will be compared with the next aircraft, it must meet the predetermined minimum standards.

Lead	VFR* T	rail Aircra	ft Type	IFR Trail Aircraft Type		
Aircraft Type	Heavy	Large	Small	Heavy	Large	Small
Heavy	90	120	120	120	120	120
Large	60	60	50	60	60	60
Small	50	45	35	60	60	60

**Table 2.** Separation time minimum for departure-departure (second)

\*These are shown to appropriately represent these operations and are not regulatory in nature.

Source: Federal Aviation Administration

Lead	VFR* 1	Trail Aircra	ft Type	IFR (Wake Vortex) Trail Aircraft Type		
Aircraft Type	Heavy	Large	Small	Heavy	Large	Small
Heavy	2.7	3.6	4.5	4.0	5.0	6.0
Large	1.9	1.9	2.7	3.0	3.0	4.0
Small	1.9	1.9	1.9	3.0	3.0	3.0

Table 3. Separation time for arrival-arrival (nm)

\*These are shown to appropriately represent these operations and are not regulatory in nature.

Source: Federal Aviation Administration

The separation time in this model is formulated with  $P_{j1j2}$  which accommodates the four flight rules. This study calculates separation time using a visual basic application (VBA) in Microsoft Excel with the formulations shown in the appendix. The model display in Excel can be seen in the following figure:

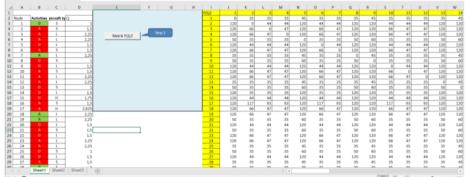


Figure 1. Matrix Calculation of P<sub>j1j2</sub>

The results of running AMPL software can be seen in Figure 2. This model is running using Gurobi 9.0.3 solver and produces a feasible solution.

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	2	413	19	2400	36	5100	53	7500	70	10263	87	13714	
	3	347	20	2700	37	5144	54	7800		10500		13594	
	4	300	21	2735	38	5210	55	8100		10582		13500	
	5	900	22	3000	39	5400	56	8899		10535		13547	
	6	935	23	3035	40	5914	57	8700		10629		13800	
	7	1200 1746	24 25	3082	41 42	5747 5700	58 59	8735 8779		11160		14299	
	9	1500	25	3350 3300	42	5794	59 60	8779 9000		11100 11466		14135 14179	
	10	1535	20	3385	43	6060	61	9300		11400		14179	
	11	1579	28	3600	44	6000	62	9335		11700		14100	
	12	1626	29	3900	46	6370		10193		12000		15000	
	13	2049	30	4285	40	6300		10143		12455		15300	
	14	1999	31	4250	48	6335	65			12300		15600	
	15	1800	32	4200	49	7114		10023		12335		15900	
	16	1835	33	4320	50	6947	67	9935	84	12900			
	17	1879	34	4500	51	6900	68	9900	85	12960			
	;												

Figure 2. AMPL Running Result

Running with alternative 1 cost of using fuel by taking into account the difference between arrival and departure and aircraft type can be seen in Figure 3 below. Whereas alternative 2 scheduling does not pay attention to the fuel cost of each type but rather prioritizes the type and type of aircraft.

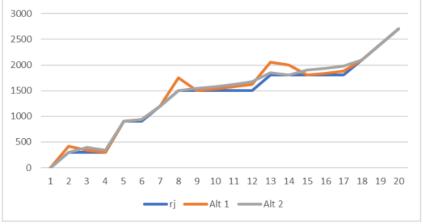


Figure 3. Alternative 20 flight schedule chart

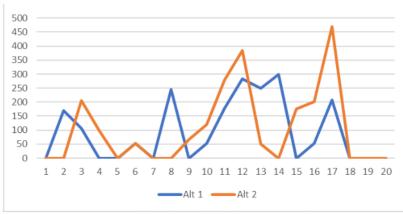


Figure 4. Graph of fuel usage consumption

Meanwhile, the results of the cost fuel generated from the 2 alternatives show that alternative 1 has lower fuel consumption compared to alternative 2.From these results, MIP can be applied in scheduling aircraft departing and arriving at the same time so as to reduce the cost of using fuel while waiting. assigned to the runway.

#### 4. CONCLUSION

This research can produce a schedule that can save the cost of using fuel on each aircraft while on the runway using mixed integer programming. By using 2 alternatives it can be compared that alternative 1 is more minimum than alternative 2. Alternative 1 considers the fuel cost of each type and type of aircraft and prioritizes arrival, while alternative 2 only considers the type and type of aircraft and is close to ready time. From these results, MIP can be applied in scheduling aircraft that depart and arrive at the same time so as to reduce the cost of using fuel while waiting to be assigned to the runway.

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